



The equilibrium equation of state of gas mixture with the detailed considering of the chemical composition

Pruel E.R.
pru@hydro.nsc.ru

Lavrentyev Institute of Hydrodynamics of the Siberian Branch of the Russian Academy of Sciences

Thermodynamic model with a frozen chemical composition

$h_i(T)$ – The enthalpy of 1 mole of matter versus temperature in the "standard state" ($p_0 = 101325$ Pa).

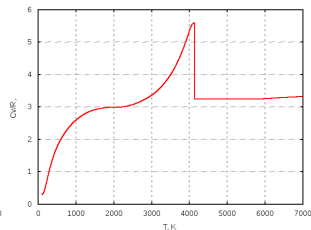
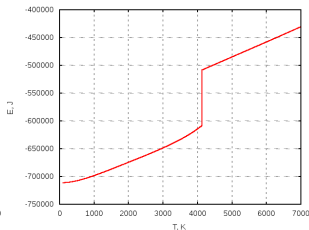
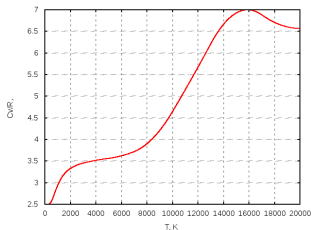
$$H(T, p) = \left[\begin{array}{l} \sum_i \nu_i h_i(T) \\ \sum_i \nu_i h_i(T) + (p - p_0) V_{cond i} \end{array} \right] \quad \text{– полная энтальпия системы.}$$

$$E(T) = \left[\begin{array}{l} \sum_i \nu_i (h_i(T) - RT) \\ \sum_i \nu_i h_i(T) - p_0 V_{cond i} \end{array} \right] \quad \text{– Total energy of the system.}$$

The density of the condensed phase is assumed to be constant.

$p = \nu_{gase} RT / V_{gase}$ – давление, где $V_{gase} = V - \sum_i V_{cond i}$.

$$c_v = \left(\frac{\partial E}{\partial T} \right)_V, \quad c_p = \left(\frac{\partial H}{\partial T} \right)_p, \quad \gamma_f = c_p / c_v, \quad c_f = (\gamma_f p / \rho)^{1/2}.$$



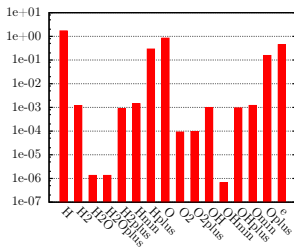
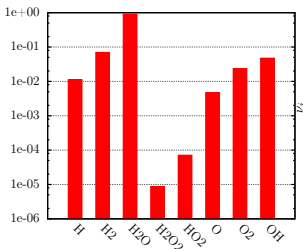
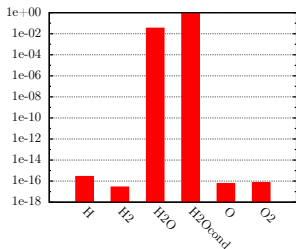
The heat capacity of nitrogen (N_2), the internal energy and heat capacity of condensed carbon (graphite, liquid carbon).

The thermodynamic model of reacting rarefied gases

$$F_i(N_i, V, T) = -kT \left[\ln \left(\left(f_i(T) V e^{-\epsilon_i/kT} \right)^{N_i} / N_i! \right) \right], F(V, T) = \sum F_i(N_i, V, T).$$

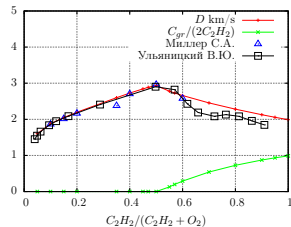
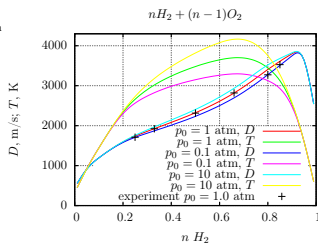
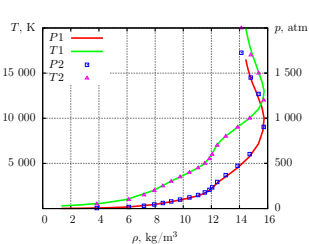
$V, T = \text{const} \min F.$

- ▶ V.P. Glushko, D. Stall.
- ▶ NIST Chemistry WebBook. Thermodynamic data for 7000 compounds.
- ▶ NASA online CEA. Thermodynamic and gas dynamic calculations for 2000 compounds.



Equilibrium chemical concentrations of a mixture of gases with a composition of $2H + O$ (water) at a temperature of 300, 3000 and 20 000 K. The density is 1 kg/m^3 .

Testing for gas-dynamic flows: shock and detonation waves

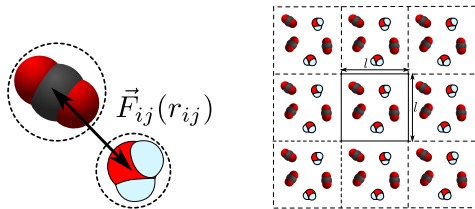


Shock wave in the atmosphere. Detonation of mixtures of hydrogen and acetylene with oxygen ($D = u + c$).

www.ancient.hydro.nsc.ru/chem. Shock and detonation waves, gas suspension, the possibility of forming gas components: Ar, Ar⁺, C₂, C₂H₂, C₂H₄, C₂H₆, C₂⁻, C₂N₂, C₂⁺, C₃, C₃H₈, C₄, C₄H₁₀, C₅, C_{cond}, C, CH₄, CH, C⁻, CN, CO₂, CO₂⁺, CO, CO⁺, C⁺, e, H₂, H₂O₂, H₂O_{cond}, H₂O, H₂O⁺, H₂⁺, H₃O⁺, H₃⁺, H, He, He⁺, H⁻, HO₂, HO₂⁻, H⁺, N₂, N₂O₃, N₂O₄, N₂O₅, N₂O, N₂⁺, N₃, N, NH₃, NO₂, NO₂⁻, NO₃⁻, NO, NO⁺, N⁺, O₂, O₂⁻, O₂⁺, O₃, O, OH, OH⁻, OH⁺, O⁻, O⁺, Si₂C, Si₂, Si₃, SiC₂, SiC_{cond}, SiC, SiC_{gase}, SiC_{liq}, Si_{cond}, Si, Si_{gase}, SiH₂, SiH₃, SiH₄, SiH, S_{liq}, SiN, SiO₂cond, SiO₂, SiO₂gase, SiO₂liq, SiO, Si⁺;

and condensed phases C, H₂O, SiO₂, Fe, FeO, Fe₂O₃, Fe₃O₄, FeS, FeS₂.

A mixture of reacting dense gases. The Monte Carlo Method



The free energy of internal degrees of freedom: rotation, oscillations, and electronic excitations depends only on temperature.

$$W = \prod_i ((f_i(T)V)^{N_i}/N_i!) e^{-U(\vec{r}_1, \dots, \vec{r}_i)/kT}, \quad W_{p,q} \sim W_q/W_p.$$

- ▶ Change in chemical composition according to the balance of the reaction.
- ▶ Displacement of particles: random or according to the laws of mechanics.
- ▶ Acceptance or rejection of a new state.

$$U = 4\epsilon \left(\left(\frac{b}{r}\right)^{12} - \left(\frac{b}{r}\right)^6 \right) - \text{the Lennard-Jones potential,}$$

$$U_{\text{exp-6}} = \frac{\epsilon}{1-6/\alpha} \left(\left(\frac{6}{\alpha}\right) \exp \left[\alpha \left(1 - \frac{r}{b}\right) \right] - \left(\frac{b}{r}\right)^6 \right) - \text{exp-6 potential.}$$

$C, C_{\text{cond}}, O, O_2, H, H_2, N, N_2, NO, CO, CO_2, H_2O, OH, CH_4, NH_3.$

Calculation of thermodynamic parameters.

$$PV = NkT - 1/6 \sum_{i=1}^N \sum_{j \neq i}^{\infty} r_{ij} F(r_{ij}), \quad E = 1/2 \sum_{i=1}^N \sum_{j \neq i}^{\infty} U(r_{ij}) + \sum_{i=1}^N N_i e_i(T).$$

Calculation of the thermodynamic characteristics of the system

Calculated by the Monte Carlo method: $p(\rho, T)$, $E(\rho, T)$.

Calculated numerically: $\left(\frac{\partial p}{\partial \rho}\right)_T$, $\left(\frac{\partial p}{\partial T}\right)_\rho$, $\left(\frac{\partial E}{\partial \rho}\right)_T$, $\left(\frac{\partial E}{\partial T}\right)_\rho$.

Calculated through the appropriate thermodynamic relationships:

$$c_v = \left(\frac{\partial E}{\partial T}\right)_\rho,$$

$$c_p = c_v + \left(\frac{pm}{\rho^2} - \left(\frac{\partial E}{\partial \rho}\right)_T\right) \left(\frac{\partial p}{\partial T}\right)_\rho / \left(\frac{\partial p}{\partial \rho}\right)_T,$$

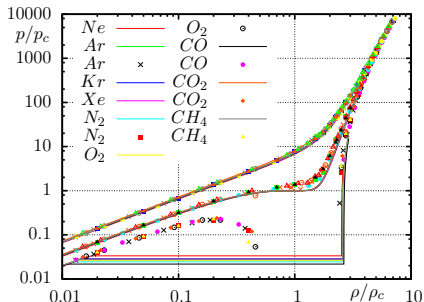
$$c_{sound} = \left(\frac{\partial p}{\partial \rho}\right)_S^{1/2} = \left(\left(\frac{\partial p}{\partial \rho}\right)_T \frac{c_p}{c_v}\right)^{1/2},$$

$$\gamma = \left(\frac{\partial p}{\partial \rho}\right)_S \frac{\rho}{p} = \left(\frac{\partial p}{\partial \rho}\right)_T \frac{c_p}{c_v} \frac{\rho}{p}.$$

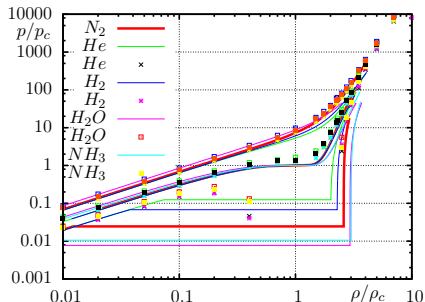
Potential calibration. Critical point

$$k_B T_c / \varepsilon = 1.326, \rho_c b^3 / m = 0.316.$$

$$T = 0.6T_c, T_c, 2T_c$$



$$T = 0.6T_c, T_c, 2T_c$$



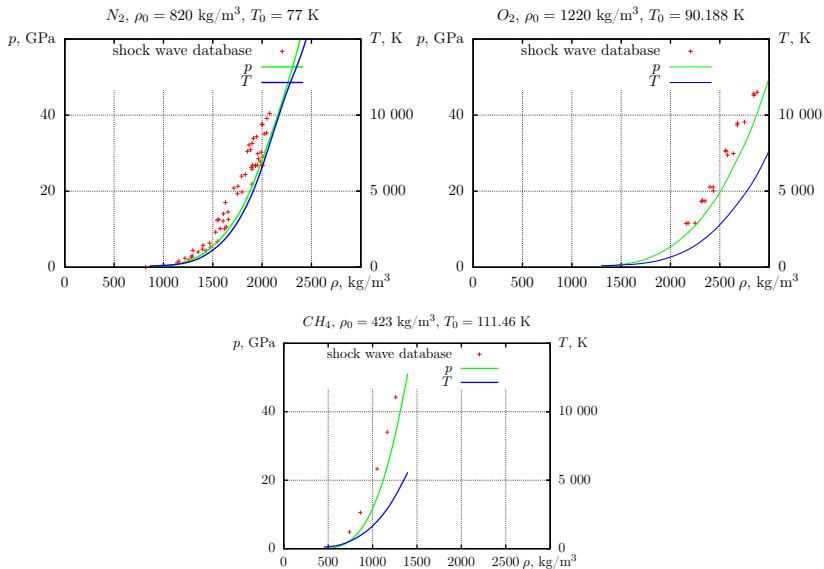
"Good" material.

Problems: quantum effects for light gases, polar molecules, phase separation, no ionization.

Calibration range: pressure from "0" to 1 GPa, temperature 100 - 10 000 K.

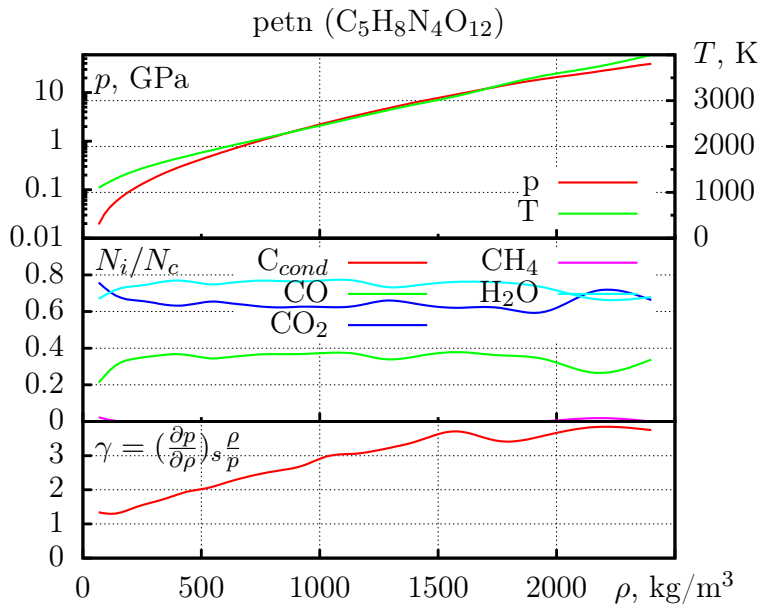
"Bad" material.

Potential calibration. Shock Waves

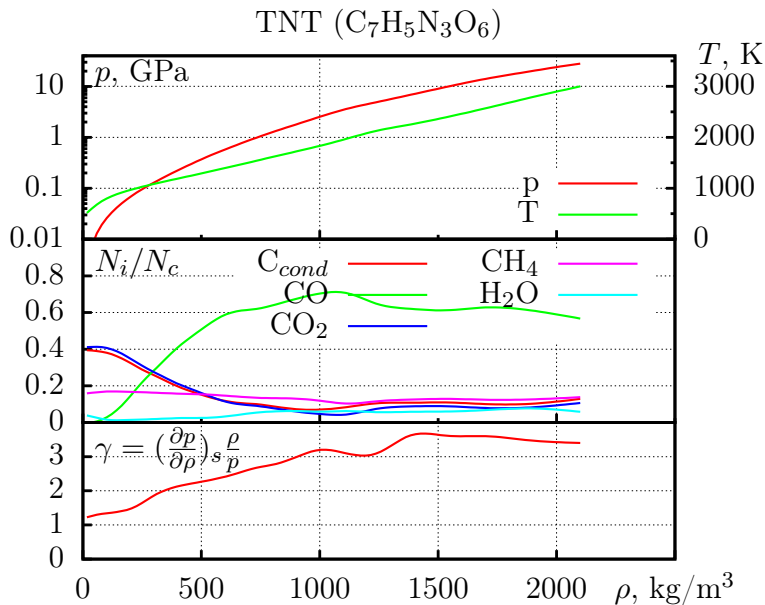


It is not possible to describe the entire range with a single set of potential parameters. For low pressures, Lennard-Jones, for high exp-6.

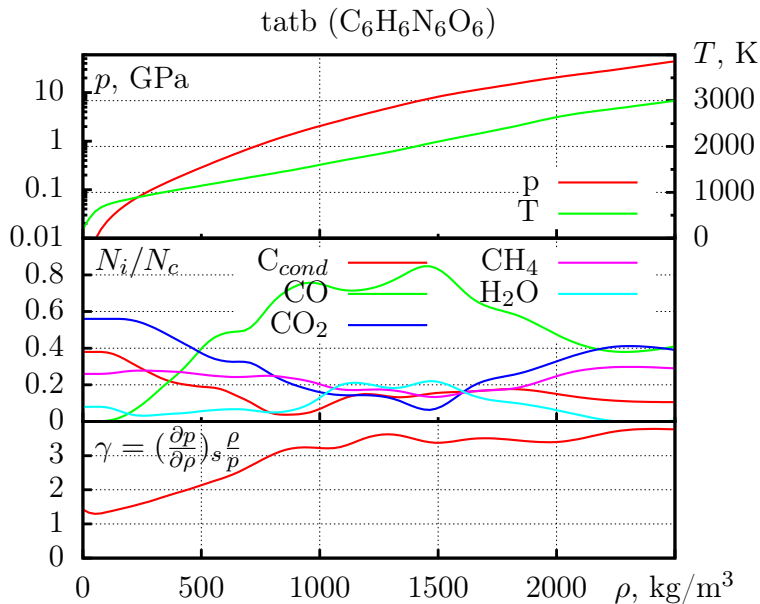
Adiabat unloading of detonation products (petn, $\rho_0 = 1770 \text{ kg/m}^3$)



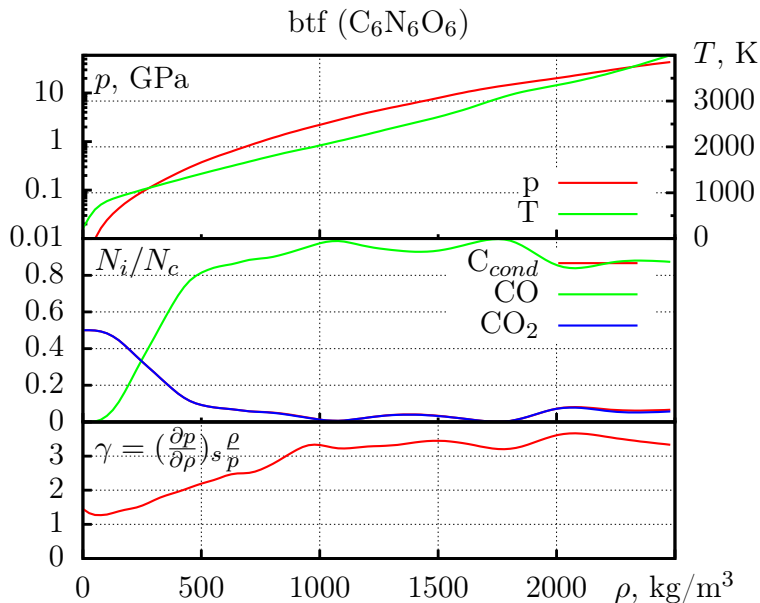
Adiabat unloading of detonation products (tnt, $\rho_0 = 1600 \text{ kg/m}^3$)



Adiabat unloading of detonation products (tatb, $\rho_0 = 1860 \text{ kg/m}^3$)



Adiabatic unloading of detonation products (benzo three furoxane, $\rho_0 = 1860$ kg/m³)



Conclusion

- ▶ A thermodynamic model of dense reacting gases was realized.
- ▶ Its testing (phase transitions, shock waves, adiabats of unloading detonation products) has been carried out.
- ▶ Achievements and issues identified.
- ▶ <http://ancient.hydro.nsc.ru/chem>.